

Reliability Analysis of River Embankments --using analytical methods and finite elements--

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Funding



Project Management



Coordination



Benefits of reliability analysis

Aim of a reliability analysis in river flood protection

Systematic determination of flood risk as cost-benefit-analysis

Risk = Failure probability x Consequence

Not: „This is a potential weak spot!“

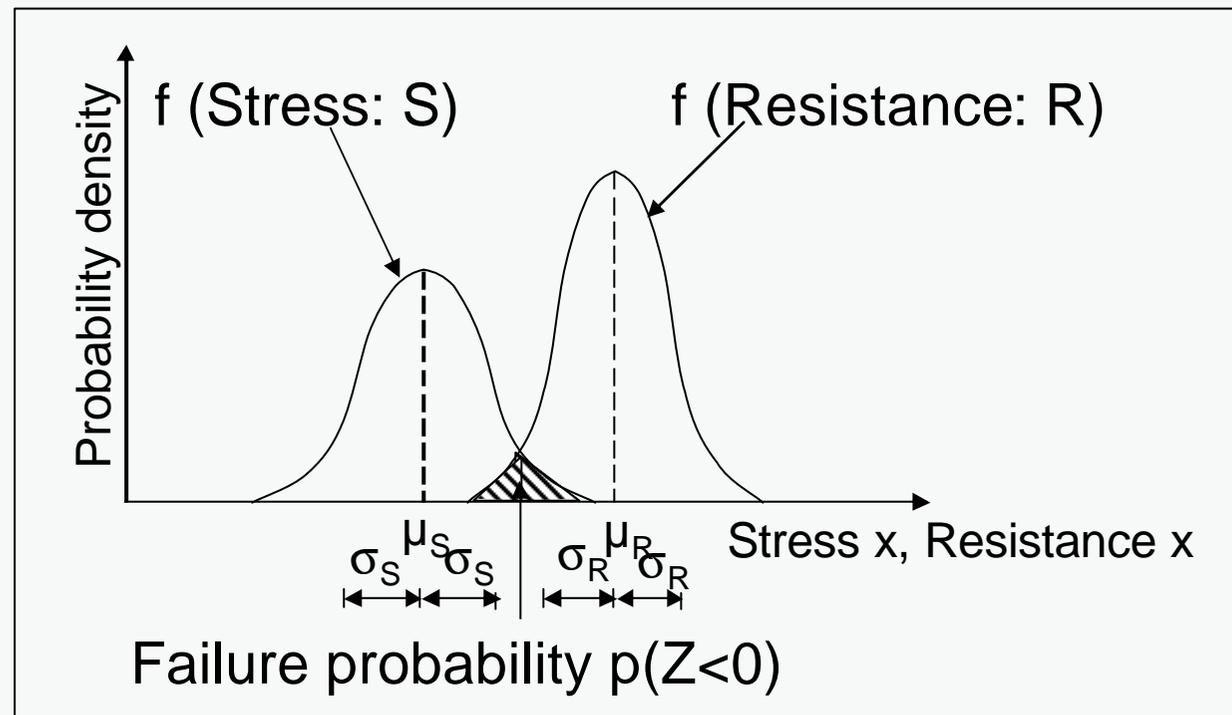
But: „Those are the sections to start improving the flood protection.“

And: „Those are the most cost-efficient measures.“

- Introduction into reliability analysis
- Case study Elbe river
- Probabilistic Finite-Element Analysis of embankment stability
- Conclusions and Outlook

Introduction into reliability analysis

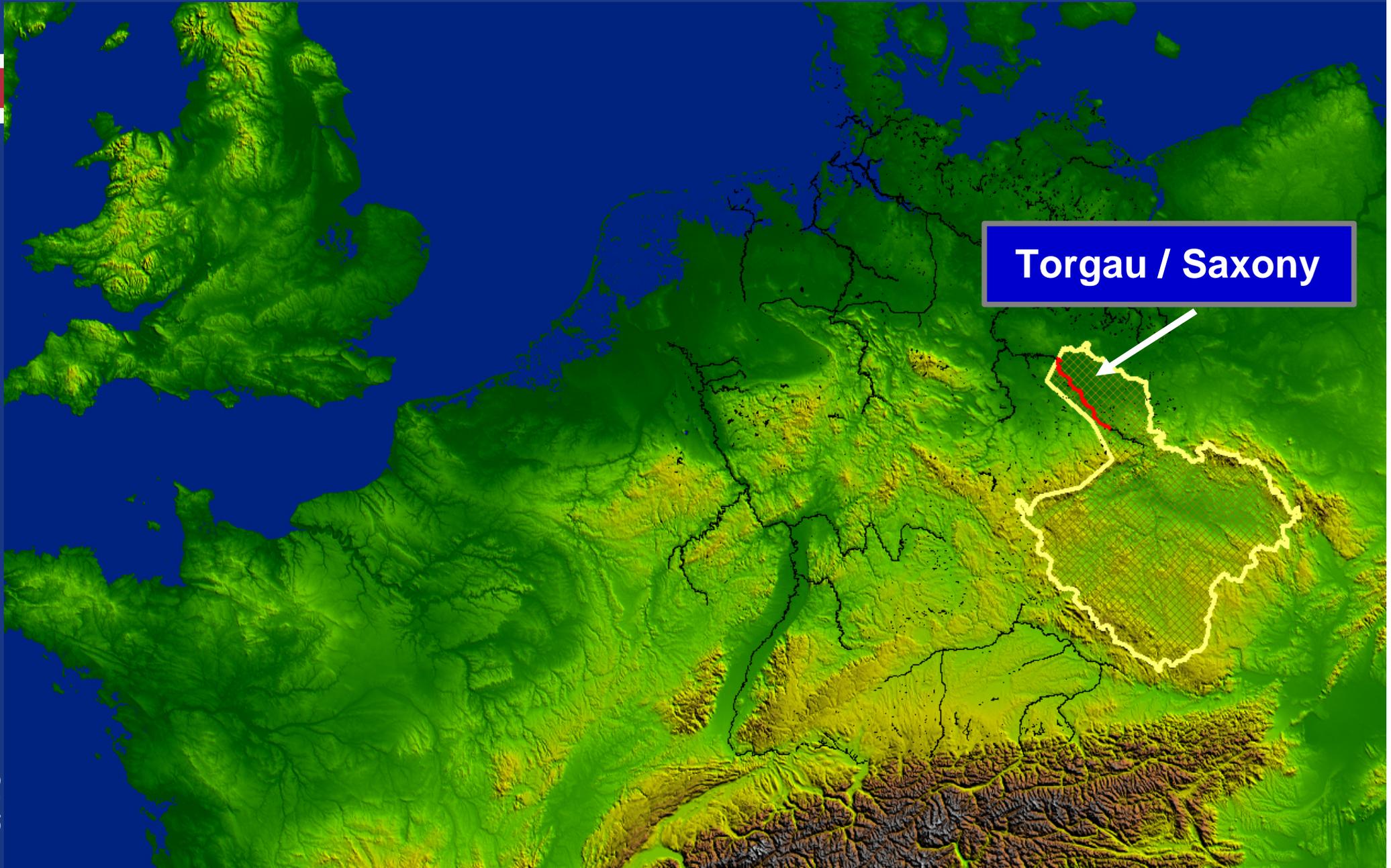
Limit state equation: $Z = R - S$ R: Resistance, S: Stress



Reliability index for Gaussian (normally) distributed variables and $Z = R - S$:

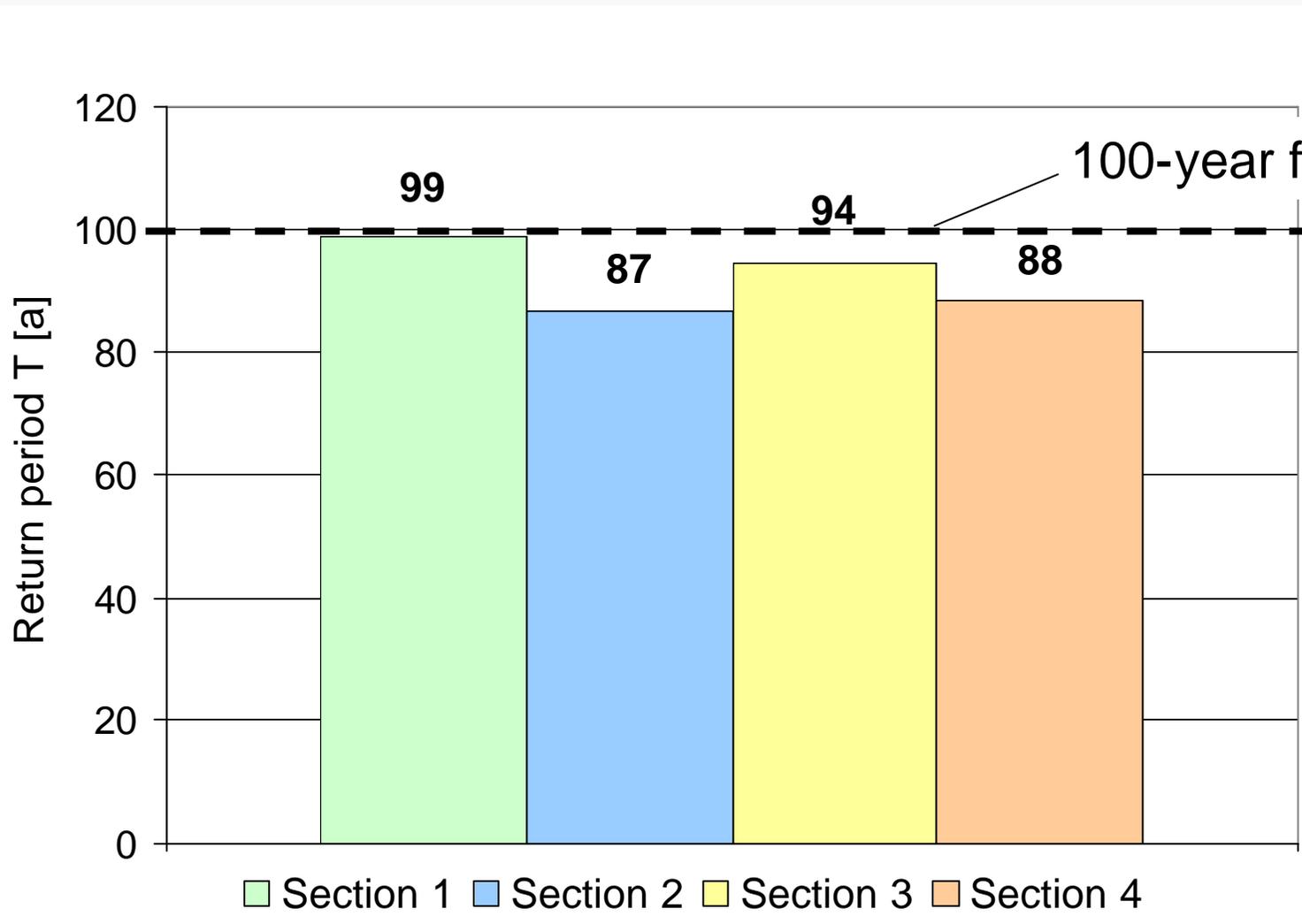
$$\beta = \frac{\mu_R - \mu_S}{\sqrt{\sigma_R^2 + \sigma_S^2}} = \frac{\mu_Z}{\sigma_Z}$$

Case study Elbe river



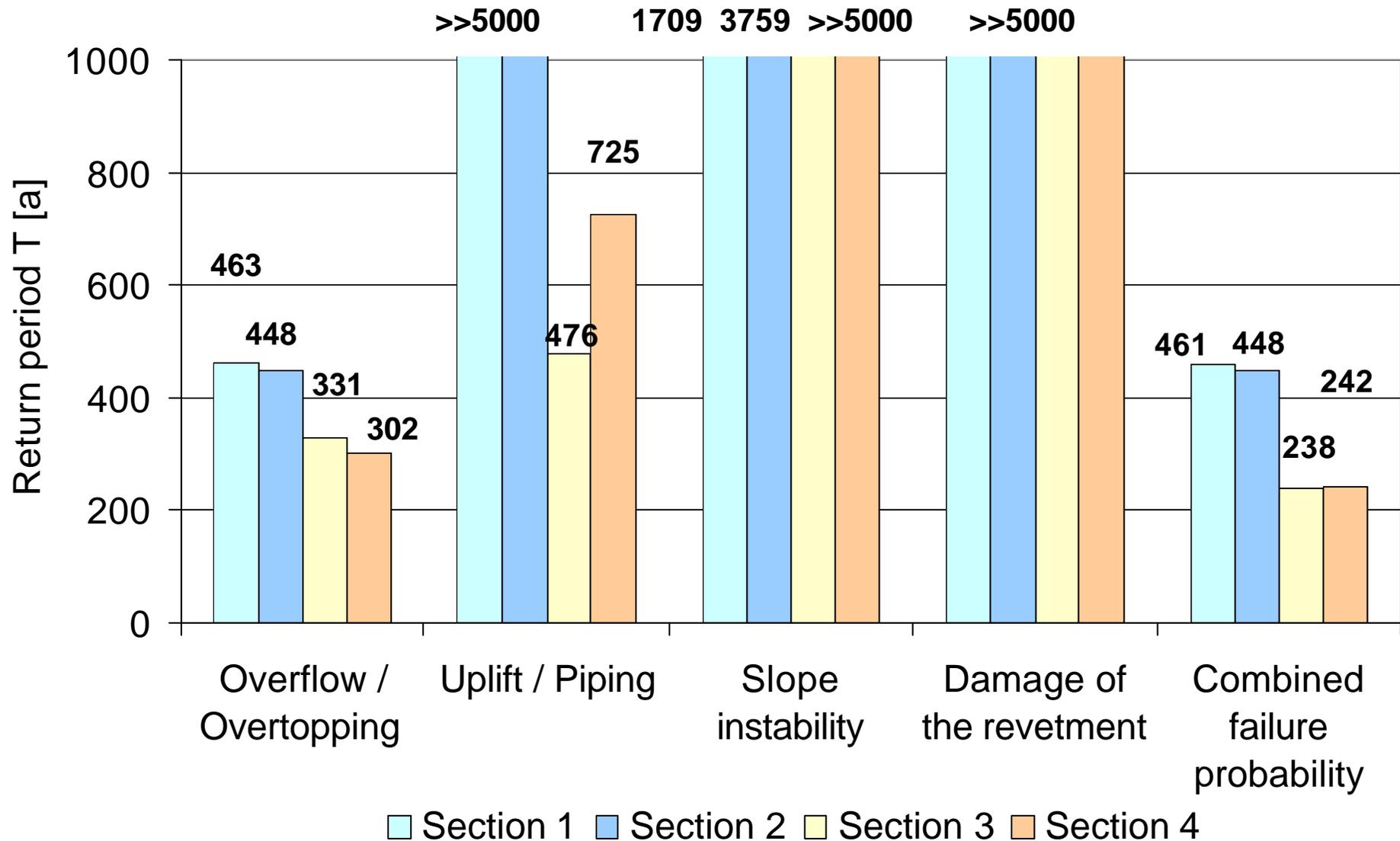
Case study Elbe river

Comparison to a 100-year flood only considering overflow (Dike stretch B)



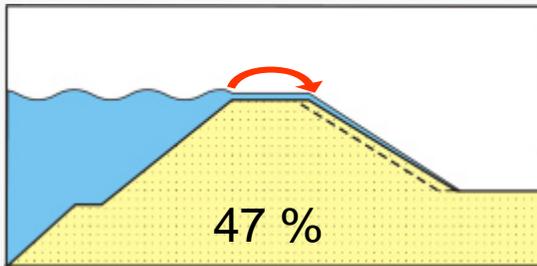
Case study Elbe river

Computed failure probabilities for dike stretch B

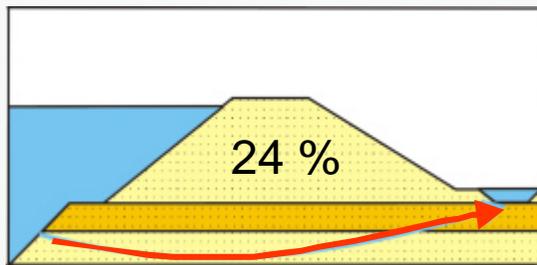


Case study Elbe river

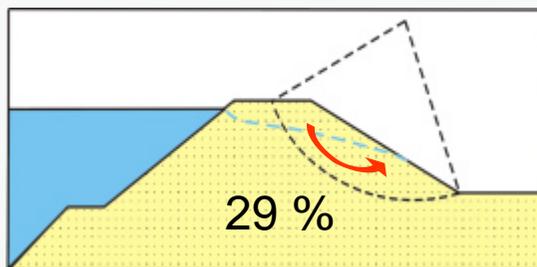
Comparison to Elbe flood 2002 - dike failure statistics (Horlacher, 2005)



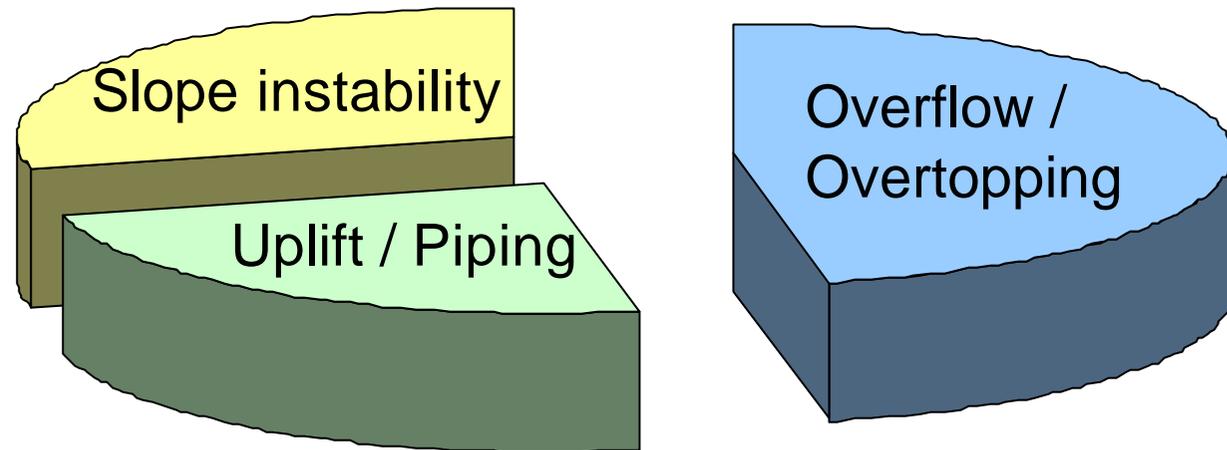
Overflow / Overtopping



Uplift / Piping

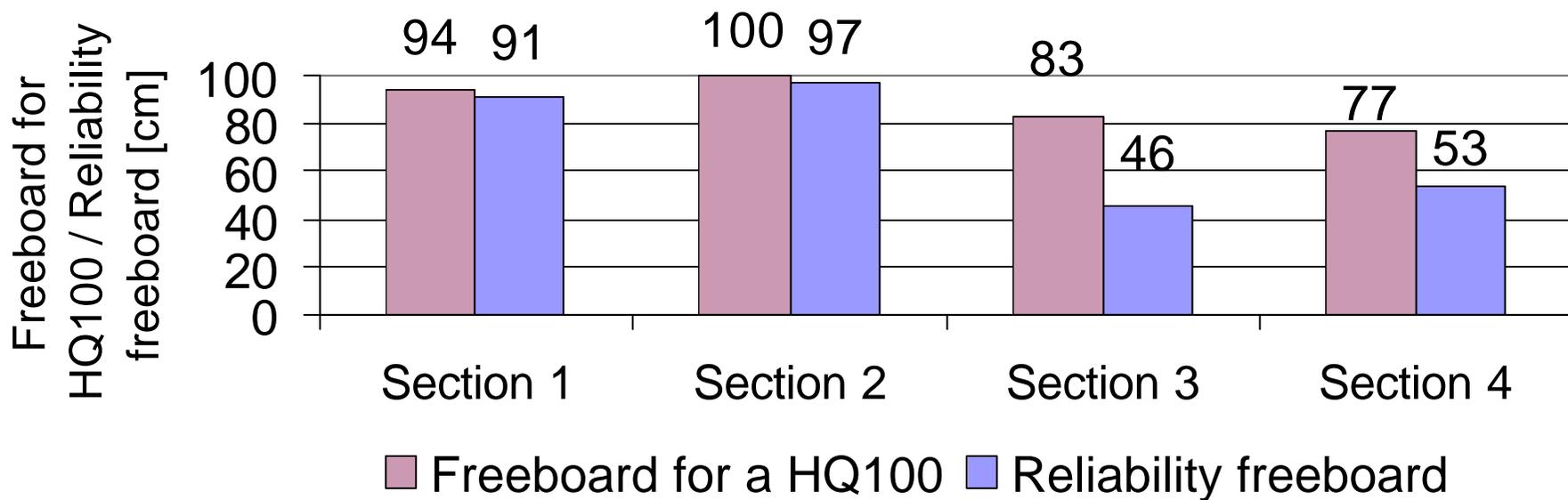
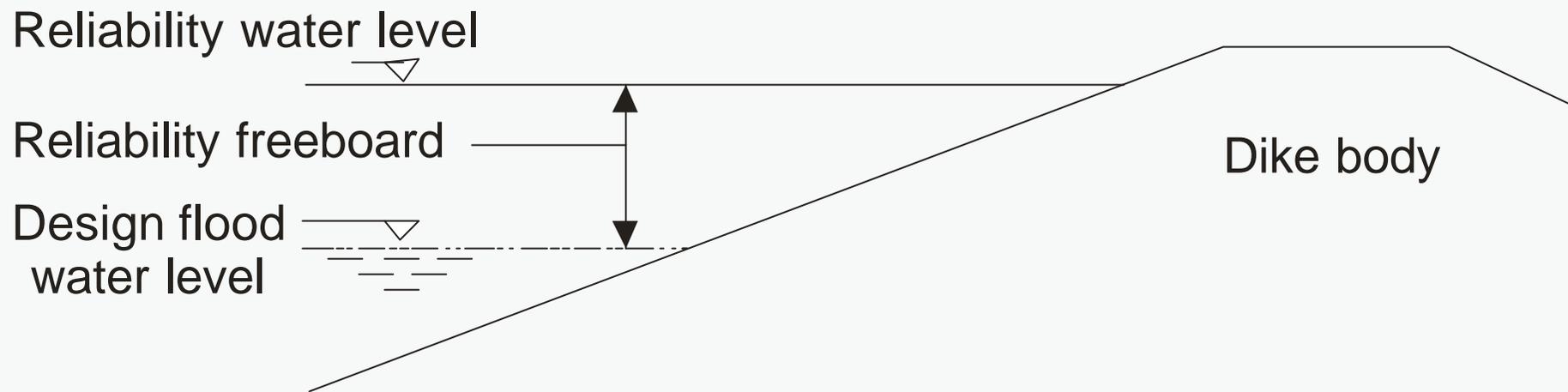


Slope instability

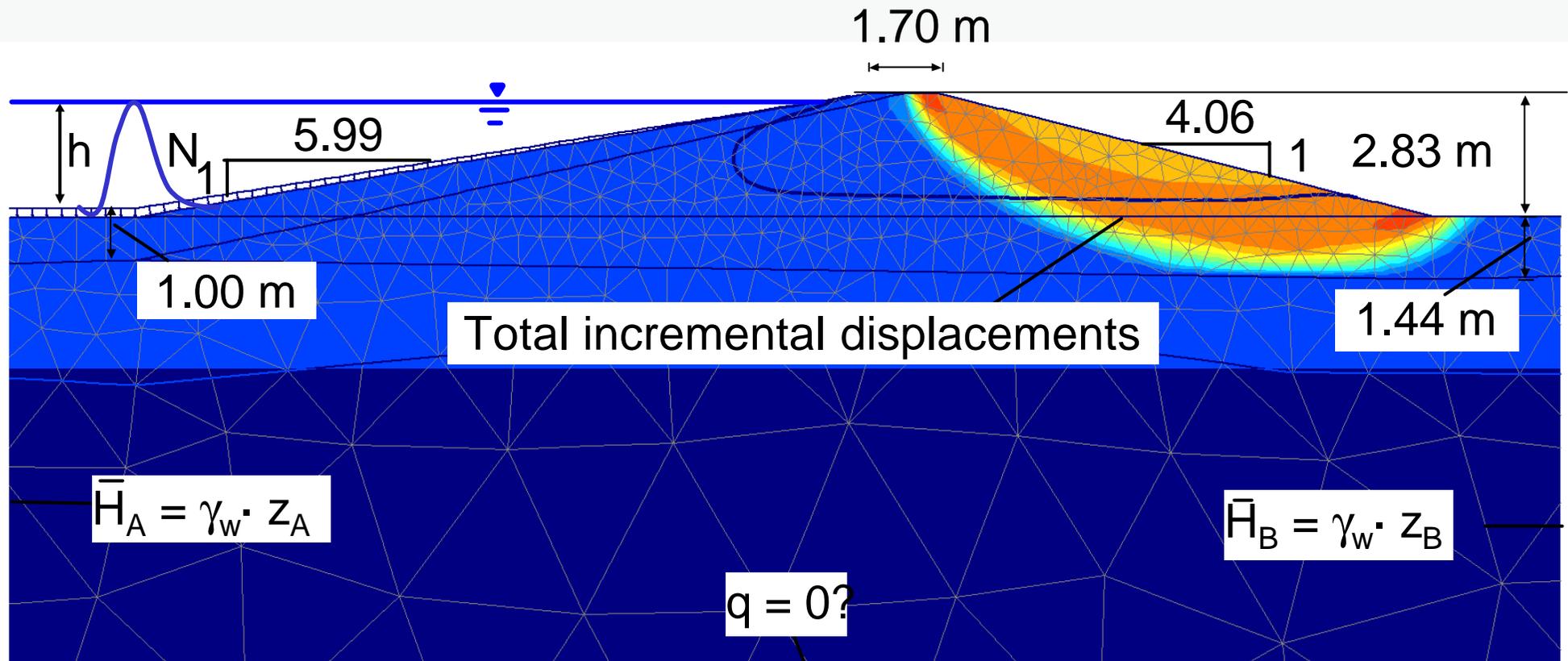


Failure mode	Dike failure statistics	Relative failure probability (PC-Ring)
Overflow / Overtopping	47 %	66 %
Uplift / Piping	24 %	28 %
Slope instability	29 %	6 %

Reliability water level and reliability freeboard



Probabilistic Finite-Element Analysis of embankment stability

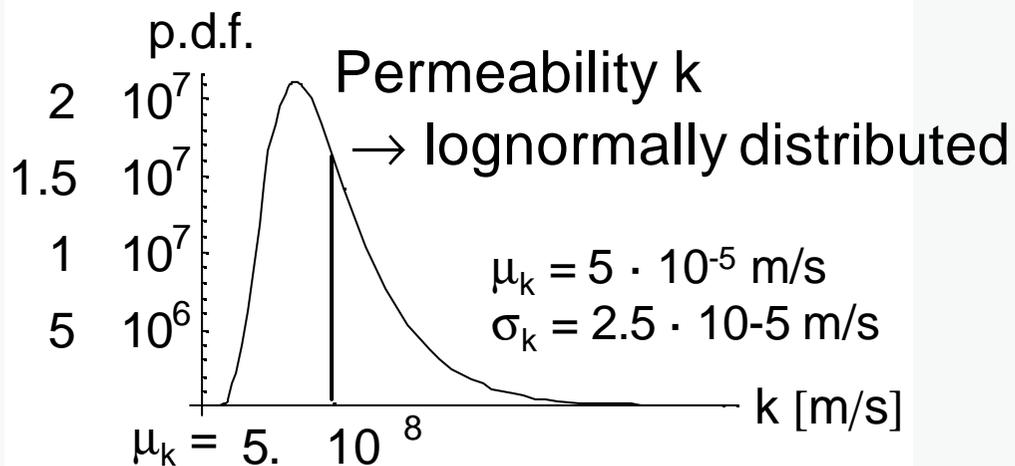
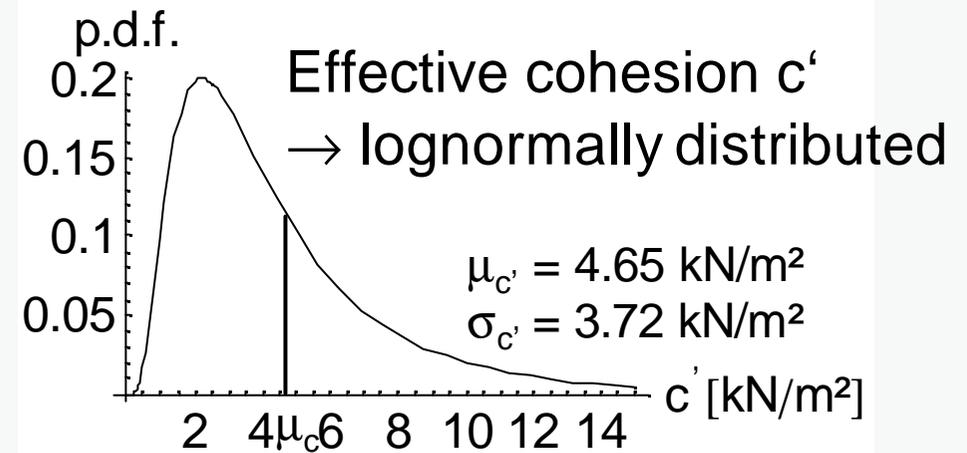
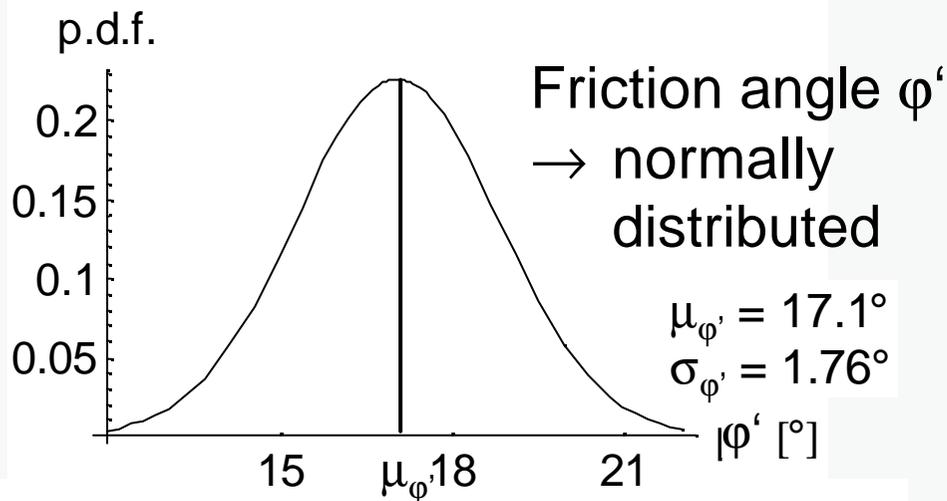


Benefits:

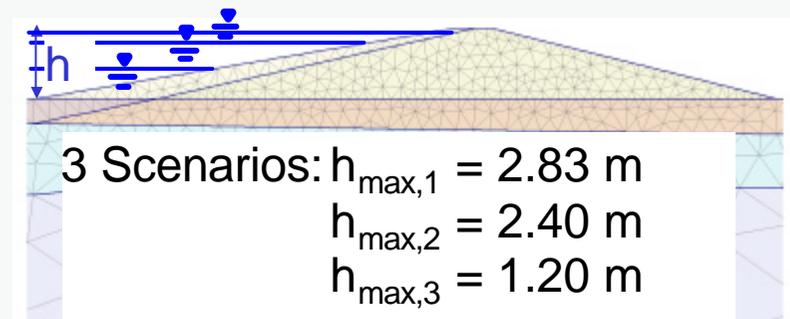
- Stability reserves due to transient seepage effects can be quantified.
- Zoned dike structure can be taken into account.

Probabilistic Finite-Element Analysis of embankment stability

Stochastic input parameters



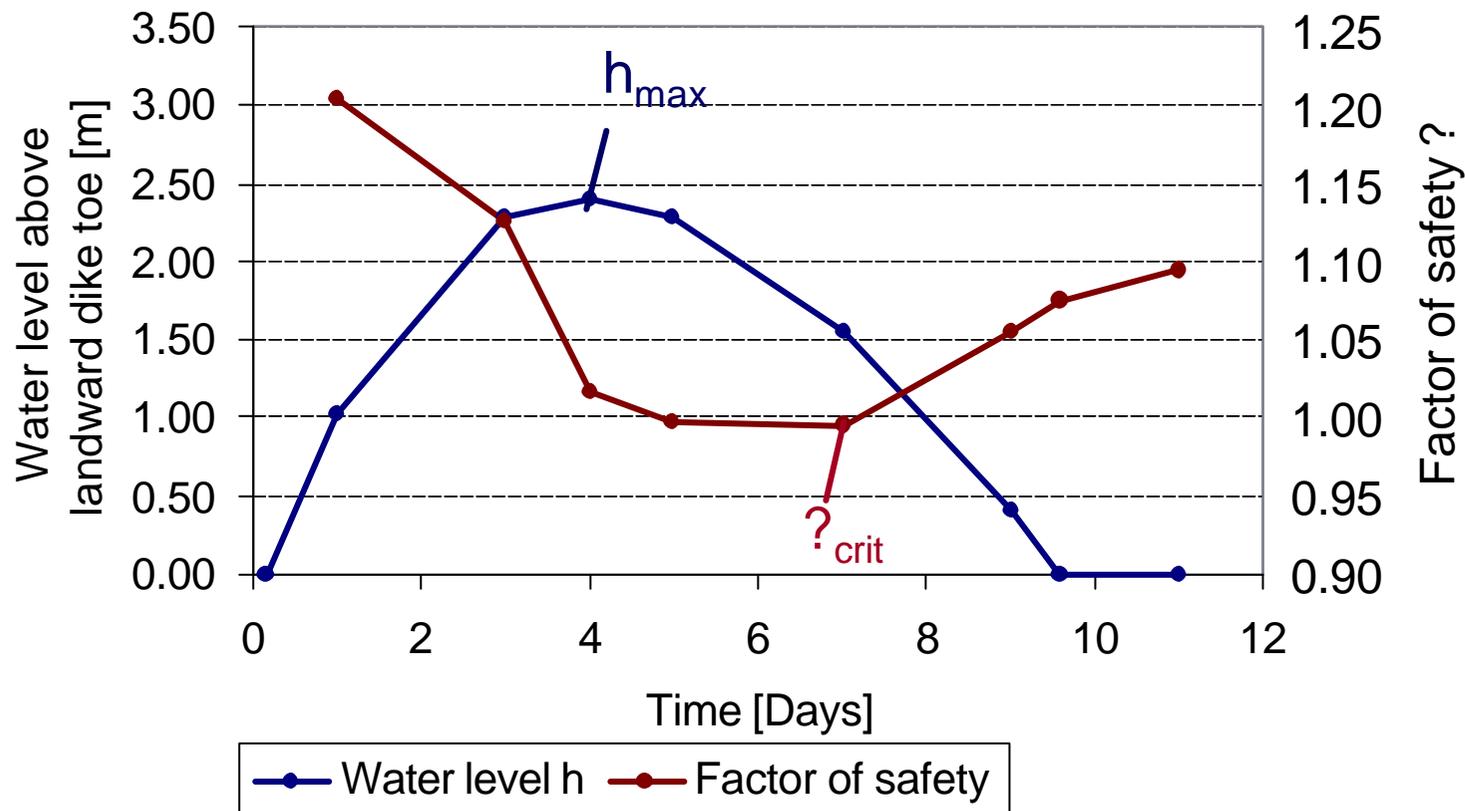
→ Correlated river water level h
and duration of the flood wave N



Probabilistic Finite-Element Analysis of embankment stability

Phase shift between maximum water level and minimum factor of safety

→ Factor of safety ? needs to be checked for various time steps
for various flow patterns



Probabilistic Finite-Element Analysis of embankment stability

First Order Reliability Method with Adaptive Response Surface (FORM-ARS)

Perform numerical simulations around mean value

Output: Factor of safety γ from a numerical stability analysis

Find best-fit Response Surface for $\gamma = b_0 + b_1 \cdot f' + b_2 \cdot c' + b_3 \cdot k$

Find design point for Response Surface

Check design point with numerical results

IF ($\gamma \sim 1$) AND IF (New design point = Old design point)

then

Determination of failure probability

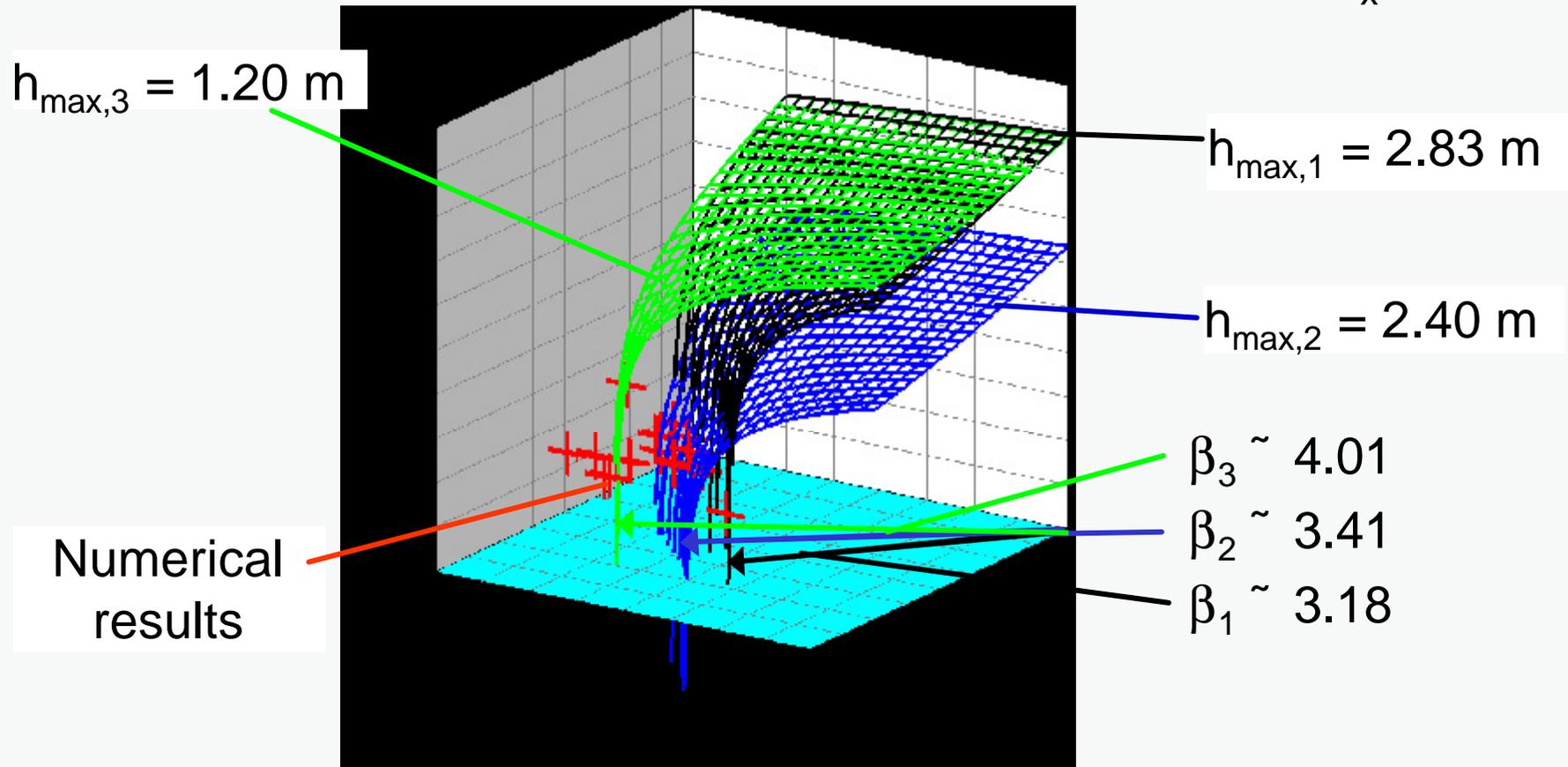
Perform numerical
simulations around
the design point

else

Probabilistic Finite-Element Analysis of embankment stability

Response Surfaces for three different maximum water levels

Transformation into standard-normalized variables:
$$u_i = \frac{X - \mu_x}{\sigma_x}$$



→ 240 Finite-Element calculations → Return period of failure: $\sim 40,000$ years

- Reliability analysis as basis for a reliable flood risk management
- Comparable tendency with dike failure statistics during the flood in 2002
- Integration of a probabilistic FE-analysis for slope instabilities which regards zoned dikes and transient seepage effects
- Provision of a tool for risk-based river flood protection
- Accompanying paper at ISFD4 2008 by Merkel and Westrich

Thank you for your attention!

Questions?

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